

SUBIR SACHDEV

Research Highlights

I. QUANTUM CRITICALITY

1. *Gapless spin-fluid ground state in a random quantum Heisenberg magnet*, S. Sachdev and J. Ye, [Physical Review Letters](#) **70**, 3339 (1993).

This was the first soluble model of a quantum critical many-body system without any quasiparticle excitations. Its impact has been diverse:

- Already in the 1993 paper, Sachdev indicated the connection to “marginal Fermi liquid” behavior in cuprates. This connection has since seen extensive developments, summarized in *Sachdev-Ye-Kitaev Models and Beyond: A Window into Non-Fermi Liquids*, D. Chowdhury, A. Georges, O. Parcollet, and S. Sachdev, [Reviews of Modern Physics](#) **94**, 035004 (2022). This work has led to the realistic models described under paper 4.
- There has been a direct and extensive impact from the theory of quantum criticality in condensed matter physics to the quantum theory of black holes via the 1993 paper by Sachdev and Ye and a paper by Sachdev in 2010 (S. Sachdev, [Physical Review Letters](#) **105**, 151602 (2010)). The latter paper was the first to point out that ‘certain mean-field gapless spin liquids’ are quantum matter states without quasiparticle excitations realizing the low energy quantum physics of charged black holes. With ‘mean-field gapless spin liquids’ Sachdev was referring to what can now be called the SYK critical state. Based on results in A. Georges, O. Parcollet, and S. Sachdev, [Physical Review B](#) **63**, 134406 (2001), Sachdev argued in the 2010 paper for a correspondence between the SYK model and charged black holes at the semiclassical level. In 2015, Kitaev (Talks at KITP, University of California, Santa Barbara) showed that the correspondence held at the fully quantum level. This connection has undergone rapid development in recent years, and has led to an understanding of the generic universal structure of the low-energy density of states of non-supersymmetric charged black holes in $D \geq 4$ spacetime dimensions (L.V. Iliesiu, S. Murthy and G.J. Turiaci, [arXiv:2209.13608](#), S. Sachdev [arXiv:2304.13744](#)). The SYK model has also been a key ingredient in the recent advances in understanding of Hawking radiation—see the review, R. Buosso *et al.*, [arXiv:2201.03096](#).
- This model was developed by A. Sengupta (A.M. Sengupta [arXiv:9707316](#), [Phys. Rev. B](#) **61**, 4041 (2000)) and Q. Si into what is now known as “extended dynamical mean field theory”, used as a model of numerous heavy fermion compounds.

2. *Non-zero temperature transport near quantum critical points*, K. Damle and S. Sachdev, [Physical Review B](#) **56**, 8714 (1997).

This paper introduced ideas on what is now often called “Planckian dynamics” in the transport of quantum critical systems. The original motivations and applications were to the superfluid-insulator

and quantum Hall transitions, but there have also been diverse applications across quantum critical systems:

- *Quantum critical transport in clean graphene*, L. Fritz, J. Schmalian, M. Müller and S. Sachdev, [Physical Review B 78, 085416 \(2008\)](#).

In what was then viewed as a surprising development, the transport properties of pure graphene were interpreted along quantum-critical lines in this paper. This led to predictions for microwave conductivity which were experimentally observed in Gallagher *et al.* [Science 364, 158 \(2019\)](#). Müller and Sachdev ([Physical Review B 78, 115419 \(2008\)](#)) were the first to propose that graphene should display hydrodynamic transport near charge neutrality. This is now a flourishing subject with many experimental studies of hydrodynamics in two-dimensional materials, especially graphene *e.g.* Mark Ku *et al.*, [Nature 583, 537 \(2020\)](#).

- *Quantum critical transport, duality, and M-theory*, C. P. Herzog, P. Kovtun, S. Sachdev, and D. T. Son, [Physical Review D 75, 085020 \(2007\)](#).

Theory of the Nernst effect near quantum phase transitions in condensed matter and in dyonic black holes, S. A. Hartnoll, P. K. Kovtun, M. Müller, and S. Sachdev, [Physical Review B 76, 144502 \(2007\)](#).

The Damle-Sachdev paper motivated holographic models of transport in quantum-critical matter in these papers. This led to extensive work on holographic theories of strongly interacting matter, as reviewed in the book *Holographic Quantum Matter* by S. Hartnoll, A. Lucas, and S. Sachdev. It also led to the realization that transport in *clean* quantum critical systems is in the strong drag limit. A recent consequence has been a reconsideration of the structure of the optical conductivity of critical Fermi surfaces: in particular, such systems only display Drude d.c. conductivity, and do not have a high frequency tail.

3. *Fractionalized Fermi liquids*, T. Senthil, S. Sachdev, and M. Vojta, [Physical Review Letters 90, 216403 \(2003\)](#).

Weak magnetism and non-Fermi liquids near heavy-fermion critical points, T. Senthil, M. Vojta and S. Sachdev, [Physical Review B 69, 035111 \(2004\)](#).

These papers introduced a new type of quantum phase transition in metals: one without any broken symmetry, involving a change in volume of the Fermi surface. It was also argued that the phase with the non-Luttinger volume (FL*) must have ‘topological’ features involving fractionalized excitations and emergent gauge fields. The quantum critical point also features these fractionalized excitations, and was an early example of a ‘deconfined quantum critical point’. These ideas have had extensive application in the study of intermetallic compounds *e.g.* in CeCoIn₅ by Maksimovic *et al.*, [Science 375, 76 \(2021\)](#).

4. *Universal theory of strange metals from spatially random interactions*, A. A. Patel, Haoyu Guo, I. Esterlis, and S. Sachdev, [Science 381, 790 \(2023\)](#).

Localization of overdamped bosonic modes and transport in strange metals, A. A. Patel, P. Lunts, and S. Sachdev, [Proceedings of the National Academy of Sciences 121, e2402052121 \(2024\)](#).

These papers develop a theory of quantum phase transition of two-dimensional metallic systems in the presence of random impurities. Surprisingly, the various clean Hertz-Millis classes, and also the topological transitions without broken symmetries all fall into essentially the same universality class. There is a wide intermediate temperature regime over which a two-dimensional Yukawa-SYK model applies; both bosonic and fermionic modes are extended in this regime. But at the lowest temperatures there is a crossover to a regime where the bosonic modes are localized, while fermionic modes remain extended, similar to behavior discussed near the metal-insulator transition in M. Milovanović, S. Sachdev and R. N. Bhatt, [Physical Review Letters **63**, 82 \(1989\)](#). These results are in good agreement with strange metal data in the cuprates and other compounds *e.g.* the d.c. and optical conductivity in Michon *et al.* [Nature Communications **14**, 3033 \(2023\)](#).

II. QUANTUM MAGNETISM

5. *Valence bond and spin-Peierls ground states of low dimensional quantum antiferromagnets*, N. Read and S. Sachdev, [Physical Review Letters **62**, 1694 \(1989\)](#).

Spin-Peierls, valence bond solid, and Néel ground states of low dimensional quantum antiferromagnets, N. Read and S. Sachdev, [Physical Review B **42**, 4568 \(1990\)](#).

- This paper first introduced a direct non-Landau-Ginzburg-Wilson transition between Néel and valence bond solid states on the square lattice, described by a \mathbb{CP}^1 U(1) gauge theory, and the Berry phases of monopoles. This has led to extensive developments in the theory of deconfined quantum criticality. Such a transition has been observed in $\text{SrCu}_2(\text{BO}_3)_2$ by Zayed *et al.*, [Nature Physics **13**, 962 \(2017\)](#) and Cui *et al.*, [Science **380**, 6650 \(2023\)](#).
- Established an equivalence between the QED theory of monopoles with Berry phases and the quantum dimer model on the square lattice.
- On the honeycomb lattice, the predicted valence bond solid order was of the Kekulé type. Such order has been observed in graphene by Liu *et al.*, [Science **375**, 321 \(2021\)](#) and Coissard *et al.*, [Nature **605**, 51 \(2022\)](#).

6. *Action of hedgehog-instantons in the disordered phase of the $2 + 1$ dimensional CP^{N-1} model*, G. Murthy and S. Sachdev, [Nuclear Physics B **344**, 557 \(1990\)](#).

The first computation of monopole scaling dimensions in a conformal field theory in 2+1 dimensions. The $1/N$ corrections were computed in E. Dyer, M. Mezei, S. S. Pufu and S. Sachdev, [Journal of High Energy Physics **1506** \(2015\) 037](#); [Erratum **1603** \(2016\) 111](#), and were found to be quantitatively accurate at small N by S. M. Chester, É. Dupuis, and W. Witczak-Krempa [Physical Review D **108**, L021701 \(2023\)](#).

7. *Large N expansion for frustrated quantum antiferromagnets*, N. Read and S. Sachdev, [Physical Review Letters, **66**, 1773 \(1991\)](#).

Large N expansion for frustrated and doped quantum antiferromagnets, S. Sachdev and N. Read, [International Journal of Modern Physics B, **5**, 219 \(1991\)](#).

The kagome and triangular lattice Heisenberg antiferromagnets: ordering from quantum fluctuations and quantum-disordered ground states with unconfined bosonic spinons, S. Sachdev, [Physical Review B **45**, 12377 \(1992\)](#).

The first proposal of a fractionalized state of quantum matter not requiring broken time-reversal symmetry. This is now called the \mathbb{Z}_2 spin liquid, and its topological and anyon properties were described. The extension to triangular and kagome lattices was presented in Evidence for a \mathbb{Z}_2 spin liquid in the triangular lattice compound KYbSe₂ was presented by Scheie *et al.*, [Nature Physics **20**, 74 \(2024\)](#).; see also paper 20. It was argued that quantum dimer models on the triangular and kagome lattices exhibit \mathbb{Z}_2 spin liquid phases.

8. *Spontaneous alignment of frustrated bonds in an anisotropic, three dimensional Ising model*, R. Jalabert and S. Sachdev, [Physical Review B **44**, 686 \(1991\)](#).

This paper showed that it is the ‘odd’ \mathbb{Z}_2 spin liquid which describes the short-range resonating valence bond state of Anderson; translations in the x and y directions anti-commute in m -particle super-selection sector in such a \mathbb{Z}_2 spin liquid. Details of the computation were published in S. Sachdev and M. Vojta, Journal of the Physical Society of Japan **69** Supplement B, 1 (2000); see the arXiv version [arXiv:9910231](#) for notes from 1991. Also gave an example of an anyon condensation transition, with the condensation of the m -particle describing the transition from the \mathbb{Z}_2 spin liquid to the valence bond solid. This is an early realization of a deconfined quantum critical point, in the XY* universality class.

9. *Universal magnetic properties of frustrated quantum antiferromagnets in two dimensions*, A. V. Chubukov, T. Senthil, and S. Sachdev, [Physical Review Letters **72**, 2089 \(1994\)](#).

Another early example of an anyon condensation transition, with the condensation of the e -particle describing the transition from the \mathbb{Z}_2 spin liquid to the non-collinear antiferromagnet. This is a deconfined quantum critical point, in the O(4)* universality class, and relates to the observations of Scheie *et al.*, [Nature Physics **20**, 74 \(2024\)](#).

10. *Low temperature spin diffusion in the one-dimensional quantum O(3) nonlinear σ -model* S. Sachdev and K. Damle, [Physical Review Letters **78**, 943 \(1997\)](#).

Spin dynamics and transport in gapped one-dimensional Heisenberg antiferromagnets at nonzero temperatures, K. Damle and S. Sachdev, [Physical Review B **57**, 8307 \(1998\)](#).

Provided an exact description of low temperature transport and damping in one-dimensional quantum systems with an energy gap. Compared quantitatively to experiments in M. Takigawa *et al.*, [Physical Review Letters **76**, 2173 \(1996\)](#), G. Xu *et al.*, [Science **317**, 1049 \(2007\)](#), and A. W. Kinross *et al.*, [Physical Review X **4**, 031008 \(2014\)](#).

11. *Quantum impurity in a nearly-critical two dimensional antiferromagnet*, S. Sachdev, C. Buragohain and M. Vojta, [Science **286**, 2479 \(1999\)](#).

Spectral function of a localized fermion coupled to the Wilson-Fisher conformal field theory, A. Allais and S. Sachdev, [Physical Review B **90**, 035131 \(2014\)](#).

The traditional Kondo effect involves a local quantum degree of freedom interacting with a Fermi

liquid or Luttinger liquid in the bulk. These papers described cases where the bulk was a strongly-interacting critical state without quasiparticle excitations, leading to novel boundary conformal field theories. The impurity was characterized by a Curie susceptibility of an irrational spin, and a boundary entropy of an irrational number of states.

12. *Landau theory of quantum spin glasses of rotors and Ising spins*, N. Read, S. Sachdev, and J. Ye, [Physical Review B](#), **52**, 384 (1995).
Equilibrium dynamics of infinite-range quantum spin glasses in a field, M. Tikhonovskaya, S. Sachdev, and R. Samajdar, [arXiv:2309.03255](#).

Theory of the infinite-range quantum Ising and rotor spin glasses, describing the transition from a ‘trivial’ quantum paramagnet to a quantum spin glass state with replica symmetry breaking. First papers to obtain the dynamic spin spectrum within the spin glass state.

III. SUPERCONDUCTIVITY

13. *Sign-problem-free quantum Monte Carlo of the onset of antiferromagnetism in metals*, E. Berg, M. A. Metlitski and S. Sachdev, [Science](#) **338**, 1606 (2012).

Showed that many quantum critical models of physical interest were amenable to quantum Monte Carlo studies. This method has been used extensively, and has led to the demonstration of superconductivity near the onset of spin density wave order.

14. *Electronic spectra with paramagnon fractionalization in the single band Hubbard model*, E. Mascot, A. Nikolaenko, M. Tikhonovskaya, Ya-Hui Zhang, D. K. Morr, and S. Sachdev, [Physical Review B](#) **105**, 075146 (2022).

Microscopic theory of the pseudogap metal phase of the hole-doped cuprates. Compared to photoemission experiments of He *et al.*, [Science](#) **331**, 1579 (2011) and Chen *et al.* [Science](#) **366**, 1099 (2019). The pseudogap phase has pocket Fermi surfaces of conventional quasiparticles with charge $+e$ and spin $1/2$, but enclosing a non-Luttinger volume, as originally described in S. Sachdev, [Physical Review B](#) **49**, 6770 (1994). The theory was based on the ancilla model of doped Mott insulators proposed by Ya-Hui Zhang and S. Sachdev, [Physical Review Research](#) **2**, 023172 (2020), which can describe a FL^* phase in a single band model.

15. *Resonant thermal Hall effect of phonons coupled to dynamical defects*, Haoyu Guo, D. G. Joshi, and S. Sachdev, [Proceedings of the National Academy of Sciences](#) **119**, e2215141119 (2022).

A new model of the thermal Hall effect, based upon a resonant ‘side-jump’ scattering of phonons off two-level systems realized by magnetic or other impurities. Connected to experiments on correlated electron compounds in H Guo, [Physical Review Research](#) **5**, 033197 (2023) and Ataei *et al.*, [Nature Physics](#) (2024).

16. *A model of d-wave superconductivity, antiferromagnetism, and charge order on the square lattice*, M. Christos, Zhu-Xi Luo, H. Shackleton, Ya-Hui Zhang, M. S. Scheurer, and S. Sachdev, [Proceedings of the National Academy of Sciences](#) **120**, e2302701120 (2023).

Emergence of nodal Bogoliubov quasiparticles across the transition from the pseudogap metal to the d -wave superconductor, M. Christos and S. Sachdev, [npj Quantum Materials](#) **9**, 4 (2024).

These papers describe the low temperature fate of the FL* pseudogap metal of the cuprates (paper 14). An important experimental constraint is that the low temperature phases with antiferromagnetic, superconducting and/or charge order must be qualitatively the same as the corresponding phases obtained from the Fermi liquid. Our work proposes that the spin liquid of the FL* phase is the SU(2) gauge theory of the π -flux spin liquid, dual to the \mathbb{CP}^1 spin liquid (paper 5), and it undergoes confinement at low temperature. This is shown to lead to a d -wave superconductor with 4 gapless Dirac points along the diagonals of the square lattice Brillouin zone (as proposed in S. Chatterjee and S. Sachdev, [Physical Review B](#) **94**, 205117 (2016)), even in cases where this region of the Brillouin zone has no Fermi surfaces in the normal state (as can be the case in the electron-doped cuprates). The SU(2) gauge theory also has charge order instabilities at an equal footing with d -wave superconductivity, and leads to states similar to those discussed in paper 7 and M. Vojta and S. Sachdev, [Physical Review Letters](#) **83**, 3916 (1999).

IV. ULTRACOLD ATOMS

17. *Mott insulators in strong electric fields*, by S. Sachdev, K. Sengupta, and S. M. Girvin, [Physical Review B](#) **66**, 075128 (2002).

Predicted that a tilted Bose-Hubbard model will have spontaneous Ising density wave order. This was observed by J. Simon *et al.*, [Nature](#) **472**, 307 (2011) and F. Meinert *et al.* [Physical Review Letters](#) **111**, 053003 (2013).

18. *Competing density-wave orders in a one-dimensional hard-boson model*, P. Fendley, K. Sengupta, and S. Sachdev, [Physical Review B](#) **69**, 075106 (2004).

Introduced the ‘FSS model’, a model of interacting hard-core bosons or qubits, related to the model in paper 17. A special case is the popular ‘PXP model’ considered by many later. The FSS model describes the blockade of Rydberg states in arrays of trapped atoms; the phase diagram predicted in this paper was observed by H. Bernien, *et al.*, [Nature](#) **551**, 579 (2017) and A. Keesling, A. Omran, H. Levine, H. Bernien, H. Pichler, Soonwon Choi, R. Samajdar, S. Schwartz, P. Silvi, S. Sachdev, P. Zoller, M. Endres, M. Greiner, V. Vuletić, and M. D. Lukin, [Nature](#) **568**, 207 (2019). The FSS model has also been proposed as a realization of universal quantum computation by Cesa and Pichler, [Physical Review Letters](#) **131**, 170601 (2023).

19. *Complex density wave orders and quantum phase transitions in a model of square-lattice Rydberg atom arrays*, R. Samajdar, Wen Wei Ho, H. Pichler, M. D. Lukin, and S. Sachdev, [Physical Review Letters](#) **124**, 103601 (2020).

Quantum Phases of Matter on a 256-Atom Programmable Quantum Simulator, S. Ebadi, Tout T. Wang, H. Levine, A. Keesling, G. Semeghini, A. Omran, D. Bluvstein, R. Samajdar, H. Pichler, Wen Wei Ho, Soonwon Choi, S. Sachdev, M. Greiner, V. Vuletić, and M. D. Lukin, [Nature](#) **595**, 227 (2021).

Predicted and observed the phase diagram of square lattice Rydberg atom arrays. Also the first experimental realization of the Ising quantum critical point in 2+1 dimensions.

20. *Quantum phases of Rydberg atoms on a kagome lattice*, R. Samajdar, Wen Wei Ho, H. Pichler, M. D. Lukin, and S. Sachdev, [Proceedings of the National Academy of Sciences](#) **118**, e2015785118 (2021).

This paper proposed that the FSS model can realize the phases of the quantum dimer model, including the \mathbb{Z}_2 spin liquid, and explored the case of the kagome lattice. An improved realization on the ruby lattice was subsequently proposed by R. Verresen *et al.*, [Phys. Rev. X](#) **11**, 031005. Quantum correlations of the \mathbb{Z}_2 spin liquid on the ruby lattice were observed by G. Semeghini, H. Levine, A. Keesling, S. Ebadi, Tout T. Wang, D. Bluvstein, R. Verresen, H. Pichler, M. Kalinowski, R. Samajdar, A. Omran, S. Sachdev, A. Vishwanath, M. Greiner, V. Vuletic, M. D. Lukin, [Science](#) **374**, 1242 (2021).